

Name:

Date:

Period:

Practice LG 4.2: Simplifying Radicals

Fully simplify the following radical expressions

a) $\sqrt{a^{10}b^{15}c^{11}}$

Remember, if no index is shown, assume that it is 2

$$\begin{array}{ccc} \sqrt{a^{10}b^{15}c^{11}} & & \\ \frac{10}{2} & \frac{15}{2} & \frac{11}{2} \\ a & b & c \\ \downarrow & \downarrow & \downarrow \\ 5R0 & 7R1 & 5R1 \end{array}$$

$$\boxed{a^5 b^7 c^5 \sqrt{bc}}$$

b) $\sqrt[3]{\frac{b^9}{b^{-5}}} = \sqrt[3]{b^{14}}$
 $= b^{14/3}$
 \downarrow
 4R2

$$\boxed{b^4 \sqrt[3]{b^2}}$$

c) $\sqrt[3]{24y^{10}}$

$$\begin{array}{ccc} \sqrt[3]{2^3 \cdot 3^1 y^{10}} & & \\ \frac{3}{3} & \frac{1}{3} & \frac{10}{3} \\ 2 & 3 & y \\ \downarrow & \downarrow & \downarrow \\ 1R0 & 0R1 & 3R1 \end{array}$$

$$\begin{array}{r} 24 \\ / \backslash \\ 8 \ 3 \\ / \backslash \\ 2 \ 2 \ 2 \\ 2^3 \cdot 3 \end{array}$$

$$\boxed{2^1 3^3 \sqrt[3]{3y^1}}$$

d) $\sqrt[3]{b^3} \cdot \sqrt[3]{8b^8} =$

$$\begin{array}{ccc} \sqrt[3]{8b^{11}} & & \\ \frac{3}{3} & \frac{11}{3} \\ 2 & b \\ \downarrow & \downarrow \\ 1R0 & 3R2 \end{array}$$

$$\boxed{2^1 b^3 \sqrt[3]{b^2}}$$

$$e) \sqrt{a^5 b^9 c^6}$$

$$\begin{array}{ccc} \frac{5}{2} & \frac{9}{2} & \frac{6}{2} \\ a \downarrow & b \downarrow & c \downarrow \\ 2R1 & 4R1 & 3R0 \end{array}$$

$$a^2 b^4 c^3 \sqrt{a^1 b^1}$$

$$f) \sqrt[5]{\frac{b^{10}}{b^{-8}}} = \sqrt[5]{\frac{b^{10} \cdot b^8}{1}}$$

$$= \sqrt[5]{b^{18}}$$

$$= b^{18/5} \quad \frac{18}{5} = 3R3$$

$$= b^3 \sqrt[5]{b^3}$$

$$g) \sqrt[3]{27x^6y^8}$$

$$\begin{array}{ccc} 3 & 6 & 8 \\ \sqrt[3]{3^3 x^6 y^8} \\ \sqrt[3]{3} & \sqrt[3]{6} & \sqrt[3]{8} \\ 3 \downarrow & \downarrow & \downarrow \\ 1R0 & 2R0 & 2R2 \end{array}$$

$$\begin{array}{c} 27 \\ / \quad \backslash \\ 9 \quad 3 \\ \textcircled{3} \quad \textcircled{3} \end{array}$$

$$3^1 x^2 y^2 \sqrt[3]{y^2}$$

$$h) \sqrt[4]{2b^3} \cdot \sqrt[4]{8b^5} = \sqrt[4]{16b^8}$$

$$\sqrt[4]{2^4 b^8}$$

$$2^{4/4} b^{8/4}$$

$$2^1 b^2$$

$$\begin{array}{c} 16 \\ \downarrow \\ 2^4 \end{array}$$